

SUBSTITUENT ELECTRONEGATIVITY PARAMETER AS THE ORIGIN OF FIELD EFFECT IN ALIPHATIC SYSTEMS

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Summary: Linear relationship between substituent electronegativity parameter ($\Delta\chi$ or σ_X) and field parameter ($\sigma_I(g)$) was obtained by using the charge separation parameter (λ) between positive and negative poles in H-X molecule calculated by *ab initio* MO method.

An elucidation of a role of group electronegativity in the field effect may cast a light on the interpretation of electronic effect of substituent in the multiparameter Hammett equation.¹ Previously we pointed out that the inductive substituent parameters (ρ) based on electronegativity were not linearly related to the field parameters (σ_I).² Recently, Reynolds³ and Taft et al.⁴ have also indicated the nonlinearity in the plot of the observed dipole moments of substituted methanes (p_{MeX}) against the group electronegativities³ and also in the plot of the substituent electronegativity parameters (σ_X), which were determined from the charge ($1 - q_H$) on the hydrogen in H-X calculated at 6-31G* level,⁴ against the substituent field parameters (σ_F).^{4b}

We wish to report here that a linear relationship between the inductive substituent ($\Delta\chi (= \chi_X - \chi_H)$)^{6c} or the substituent electronegativity parameter (σ_X)⁴ and the field parameter ($\sigma_I(g)$)⁵ defined from phenol acidities in gas phase was obtained by using the following equations,

$$\sigma_I(g) = 0.470 \cdot \Delta\chi \cdot \lambda \quad (r = 0.985, \quad n = 11) \quad (1)$$

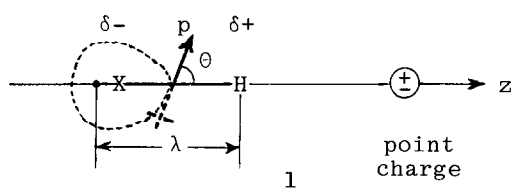
$$\sigma_I(g) = 0.972 \cdot \sigma_X \cdot \lambda \quad (r = 0.984, \quad n = 11) \quad (2)$$

where λ is the distance between positive and negative poles in H-X molecule as represented schematically in 1. The $\Delta\chi \cdot \lambda$ and $\sigma_X \cdot \lambda$ terms are proportional to the z-component of the dipole moment of H-X molecule (i.e., $p_z = p \cdot \cos\theta$; see 1). Moreover, it has been shown that the $\Delta\chi$ value, which is proportional to $\Delta\chi$ of the substituents in the same period,^{6c} is proportional to the charge ($1 - q_H$) on

Table 1. The charges on hydrogen ($1 - q_H$), z-components of dipole moments (p_z), and the distances of charge separation (λ) in H-X molecules.

| Substituent | 4-31G ^{a)} | | | 6-31G ^{a)} | | |
|-------------------|---------------------|-------------------------|---------------|---------------------|-------------------------|---------------|
| | $1 - q_H$ | p_z (D) ^{b)} | λ (Å) | $1 - q_H$ | p_z (D) ^{b)} | λ (Å) |
| CH ₃ | 0.1522 | 0.00 | 0.000 | 0.1549 | 0.00 | 0.000 |
| NH ₂ | 0.3042 | 0.73 | 0.500 | 0.3086 | 0.73 | 0.495 |
| OCH ₃ | 0.3967 | 1.24 | 0.651 | 0.3977 | 1.24 | 0.649 |
| OH | 0.3936 | 1.60 | 0.846 | 0.4257 | 1.62 | 0.796 |
| CHO | 0.1541 | 1.57 | 2.121 | 0.1484 | 1.58 | 2.221 |
| F | 0.4786 | 2.28 | 0.992 | 0.4820 | 2.30 | 0.992 |
| CF ₃ | 0.2104 | 2.17 | 2.147 | 0.1972 | 2.20 | 2.320 |
| COCH ₃ | 0.1559 | 1.20 | 1.603 | 0.1498 | 1.21 | 1.682 |
| CN | 0.3308 | 3.25 | 2.046 | 0.3336 | 3.27 | 2.039 |
| NO ₂ | 0.4320 | 3.51 | 1.692 | 0.4247 | 3.53 | 1.733 |

a) The molecular geometries were taken from experimentally determined values, (cf. ref. 6a). b) $p_z = p \cdot \cos\theta$ in Debye unit.



the hydrogen atom in the H-X molecule.^{6b}

The values of ($1 - q_H$), p_z , and λ calculated at 4-31G and 6-31G levels are given in Table 1. The $\Delta_1 \cdot \lambda$ and $\sigma_X \cdot \lambda$ values were plotted against $\sigma_I(g)$ in Fig. 1, where the average values at 4-31G and 6-31G levels were used as λ ($\lambda = p \cdot \cos\theta / [e(1 - q_H)]$). These results confirmed that the product of the substituent electro-negativity parameter, Δ_1 or σ_X , and the charge separation parameter (λ), that is, the z-component dipole moment (p_z) is the origin of the field effect in HX molecule. In fact, the following equations were obtained:

$$\sigma_I(g) = 0.192 \cdot p_z \quad \text{at 4-31G level} \\ (r = 0.988, n = 11)$$

$$\sigma_I(g) = 0.190 \cdot p_z \quad \text{at 6-31G level} \\ (r = 0.988, n = 11)$$

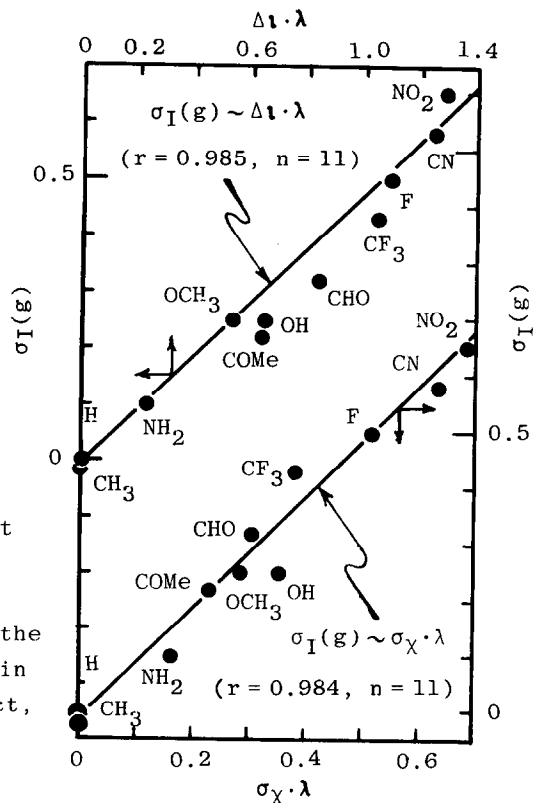


Fig. 1. Relationship between field parameter $\sigma_I(g)$ and $\Delta_1 \cdot \lambda$ or $\sigma_X \cdot \lambda$ term.

Table 2. Statistical analysis of substituent effects on acid dissociation constants ($\log(K/K_H)$) of 2 - 4.

| System | Parameter | Slope | $r^{a)}$ | SD ^{b)} | $f^{c)}$ | n |
|----------|--------------------------|-------|----------|------------------|----------|---|
| <u>2</u> | $\Delta i \cdot \lambda$ | 2.07 | 0.966 | 0.26 | 0.18 | 9 |
| | $\sigma_X \cdot \lambda$ | 3.93 | 0.957 | 0.33 | 0.19 | 9 |
| <u>3</u> | $\Delta i \cdot \lambda$ | 0.75 | 0.973 | 0.16 | 0.16 | 7 |
| | $\sigma_X \cdot \lambda$ | 1.43 | 0.973 | 0.11 | 0.17 | 7 |
| <u>4</u> | $\Delta i \cdot \lambda$ | 2.34 | 0.990 | 0.22 | 0.12 | 7 |
| | $\sigma_X \cdot \lambda$ | 4.59 | 0.991 | 0.23 | 0.12 | 7 |

a) Correlation coefficient. b) Standard deviation. c) Goodness of fit (SD/RMS). RMS denotes the root mean square of the data.

In connection with recent report,³ the acid dissociation constants of substituted acetic acids (2), 4-substituted bicyclo[2.2.2]octane-1-carboxylic acids (3), and 4-substituted quinuclidinium ion (4) were selected.³ The results of the statistical analysis of the relative dissociation constants using the new term, $\Delta i \cdot \lambda$ or $\sigma_X \cdot \lambda$, in HX are given in Table 2. They show a good correlation in each system. Therefore, the origin of the field effect^{6a} of substituent is attributed to the z-component of the dipole (i.e., $p \cdot \cos\theta$) caused by the group electronegativity of substituent.

Marriott and Topsom⁷ have recently calculated a theoretical scale of field parameter ($\sigma_F(\text{theor})$) for a wide variety of substituents by using a hypothetical proton transfer process in an isolated molecule system at a longer distance ($r = 4.5 \text{ \AA}$ or above). In order to explore the origin of the field interaction energy caused by substituent dipole close to probe center, we

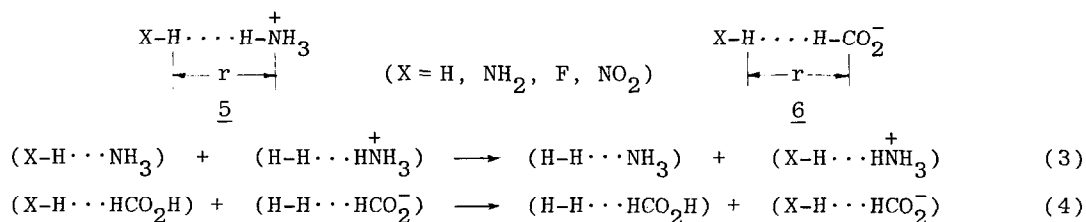


Table 3. Relative isodesmic reaction energies ($\delta\Delta E$) and its component energies^{a)} for Eqs.(3) and (4) at 4-31G level (in kcal mol⁻¹).^{b)}

| System | r (Å) | ΔΔE | ΔES | ΔPL | ΔCT | ΔEX | ΔMIX | |
|-------------------------------|-------|-------------------|--------|--------|-------|-------|-------|------|
| $\text{H}_3\text{NH}^+\cdots$ | 2.5 | H-NH ₂ | 7.64 | 8.93 | -4.69 | -3.76 | 4.53 | 2.63 |
| | | H-F | 20.98 | 23.74 | -2.95 | -3.70 | 2.43 | 1.46 |
| | | H-NO ₂ | 27.10 | 30.55 | -5.47 | -3.62 | 3.51 | 2.13 |
| $^-\text{O}_2\text{CH}\cdots$ | 2.5 | H-NH ₂ | 2.89 | -6.44 | -2.00 | -4.27 | 14.19 | 1.41 |
| | | H-F | -7.52 | -11.02 | -4.21 | -4.13 | 10.05 | 1.79 |
| | | H-NO ₂ | -12.90 | -16.50 | -6.45 | -5.27 | 12.59 | 2.73 |

a) Negative sign denotes stabilization energy. b) 1 cal = 4.184 J.

carried out the energy decomposition analysis⁸ for the relative energies ($\delta\Delta E$) of the proton transfer isodesmic reactions [Eqs. (3) and (4)] for molecular pairs 5 and 6 at various distances ($r=4.5, 3.5, 2.5, 2.25$, and 2.0 \AA) by *ab initio* MO method at 4-31G level. The distance r was taken from the H atom in H-X to the charged N atom or the carbonyl carbon atom. The relative interaction energy ($\delta\Delta E$) was divided into the five components as follows:

$$\delta\Delta E = \delta ES + \delta PL + \delta CT + \delta EX + \delta MIX$$

where the relative component energy δES means electrostatic, δPL polarization, δCT charge transfer, δEX electron exchange repulsion, and δMIX the higher order terms. Typical data of the energies ($\delta\Delta E$) and its energy components for the molecular pairs 5 and 6 are shown in Table 3 only for the case of $r=2.5 \text{ \AA}$. The δES term is generally predominant in $\delta\Delta E$, except for 6 at distances shorter than 3 \AA where the δEX term considerably contributes to $\delta\Delta E$. Figure 2 shows that the δES term in 5 and 6 correlate with the parameter, $\Delta\iota \cdot \lambda$, even in shorter distances.

Thus, it was shown that $\Delta\iota$ or σ_X is correlated with the field parameter, $\sigma_I(g)$ and σ_F , by using the charge separation parameter (λ).

This study is being extended to other substituents and systems.

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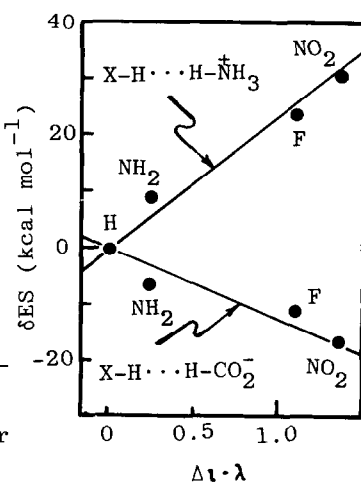


Fig. 2. Relationship between δES and $\Delta\iota \cdot \lambda$ in 5 and 6 at $r=2.5 \text{ \AA}$.